

COMPARISON OF SPAN 18M, 21M AND 24M OF T-BEAM GIRDER BRIDGE USING GRILLAGE ANALOGY METHOD

Nethravathi R¹, Dr.H Eramma², Madhukaran³, Gowda M M⁴

¹PG Student (CADS), Department of civil engineering, University of B D T College of Engineering, Davanagere, Karnataka, India

²Associate Professor, Assistant professor, Department of Studies in Civil Engineering, University.B.D.T College of Engineering Davanagere, 577004, Karnataka, India

³Assistant professor, Department of Studies in Civil Engineering, University.B.D.T College of Engineering Davanagere, 577004, Karnataka, India

⁴Structural Engineer, ALCON Consulting Engineers(INDIA) Pvt. Ltd. Bangalore, Karnataka, India

Abstract - An attempt has been made to study the behavior of T-beam bridges of their efficiency of the structure, higher stability, economy with respect to Bending moment, Shear force under standard IRC loadings. The varying span chosen for study are 18m, 21m and 24m for two lane and three lane analysis. The modelling and analysis of T-beam Girder Bridge by using SAP2000 Software and the analysis also carried out by Grillage analogy method. After analysis the results found that, In two lane analysis, Bending moment and Shear force of 31.59%,29.34%,28.49% and 25.77%,27.12%,26.12%, is more in outer girder as compared to inner girder. In three lane force analysis, Bending moment and Shear of 39.48%,27.22%,31.27% and 46.63%, 30.12% and 31.96% of 18m,21m and 24m respectively, is more in outer girder as compared to inner girder. In both two lane and three lane analysis, 17.22%,63.38% and 42.46%, 52.20% of Bending moment is more in pier cap than compared to pier. Similarly 17.22%, 63.38% and 42.46%, 52.17% of shear force is more in pier cap than compared to pier.

Key Words: T-beam, Stability, Grillage, Varying spans, SAP 2000, IRC loads.

1. INTRODUCTION

The development of country is mainly depends on agricultural and industrial activities, so, it is required to facilitate the proper transportation by providing the Flyovers and Bridges. For constructing the flyovers or the bridges we find many type of section among which T-beam bridges are very popular. T-beam girders plays very important role in motorways and system of bridges because of their efficiency of the structure, higher stability, construction, economy and aesthetical look. T-beam Bridge are considered for small and medium span bridges wheeled and tracked arrangements as shown in fig1.





WHEEL ARRANGEMENT FOR 70R (TRACKED) VEHICLE

Fig -1: Wheeled and Tracked vehicle

2.IRC Classification

2.1 Loads on bridges

The following are the various loads are to be considered

- Dead load \triangleright
- Live load
- Impact load
- Wind load \triangleright
- Longitudinal force
- **Centrifugal Forces**
- Seismic load



International Research Journal of Engineering and Technology (IRJET) RIET Volume: 05 Issue: 08 | Aug 2018 www.irjet.net

3. METHODOLOGY

The methodology used in this project is described briefly in points mentioned below.

- Modeling of a T-beam girder bridge by varying span \geq such as 18m, 21m & 24m and 12m wide across the traffic and depth of T-beam girder as 1.73, 2.03 and 2.33.
- The T-beam girder bridge is modeled with different lanes i.e. two lane and three lanes.
- The modeling of T-beam Girder Bridge is done by using SAP-2000 software.
- > The modeling of T-beam Bridge is analyzed by grillage method.
- > Then comparisons of two lanes and three lanes of Tbeam Girder Bridge are done.
- ▶ Here comparison of the bending moments, shear forces and joint reaction for grillage method.
- The modeling of peir is done by using SAP-2000 \succ software.
- \triangleright Here comparison of the base reaction, bending moments, shears forces and joint reaction for grillage method.

4.MODELLING AND ANALYSIS

Modelling and analysis of the models considered in the study using SAP 2000 software material properties are defined and assigned. Based on analysis parameters bending moments, shear forces and joint reaction for grillage method as shown in Fig 2.



Fig- 2: Dimensions of the bridge (18m span)



Fig- 3: Dimensions of the bridge (21m span)



Fig -4: Dimensions of the bridge (24m span)

Modelling for TWO and THREE lane



Fig -5: View in 3D Model with 18m span in two lane



Fig -6: View in 3D Model with 18m span in three lane



Fig -7: View in 3D Model with 21m span in two lane







International Research Journal of Engineering and Technology (IRJET) e-ISSN: 2395-0056 RIET Volume: 05 Issue: 08 | Aug 2018 www.irjet.net p-ISSN: 2395-0072



Fig -9: View in 3D Model with 24m span in two lane



Fig-10:View in 3D Model with 21m span in three lane

4.1.Modelling

It includes modelling of sub structure in Two Lane & Three Lane



Fig -11: View in 3D Model with 18m span in two lane



Fig -12: View in 3D Model with 18m span in three lane

Similar methods have to be adopted for other two spans i.e. 21m and 24m

4.2.Analysis Results

The results of models are presented and discussed in detail. The results are included for all models. Totally eight models are considered in superstructures and substructures. i.e 3 in two lane and 3in three lane. All models and results are carried out by SAP2000 Software. The results of tables and graphs are shown below.

Tabulations of Results for Superstructure:

For Two Lane analysis \triangleright

a) Bending moment

Table-1: Comparison of Bending moment for Different Spans

BENDING MOMENT (kN-M)					
OUTER GIRDER					
Combinations	ions 18m span 21m span 24m span				
Comb1 5438.41 7218.03 18330.15					
Comb2	4535.24	8166.09	16757.54		



Chart-1: Comparison of combination and Bending moment for different span

From the graph it is observed that, when the span is more the Bending moment will be more. Because when we increase length of the span changes, length of the span effects on this Bending moment. Combination -1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Bending moment value decreases for the live load Combination-2, As per IRC-6, it includes Class- A loading. The class-A loading is less compared to the 70R loading. When the vehicle load increases BM also increases.

e-ISSN: 2395-0056 p-ISSN: 2395-0072

Table-2: Comparison of Bending moment for Different
Spans

BENDING MOMENT (kN-M)				
INNER GIRDER				
Combinations18m Span21m Span24m Span				
Comb1	1078.14	1318.34	2949.63	
Comb2	865.69	1408.09	2693.46	





From the graph it is observed that, when the span is more the Bending moment will be more. Because when we increase length of the span changes, length of the span effects on this Bending moment. Combination -1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Bending moment value decreases for the live load Combination-2, As per IRC-6, it includes Class- A loading. The class-A loading is less compared to the 70R loading. When the vehicle load increases BM also increases.

b) Shear force

Table-3 : Comparison of Shear force for Different Spans

SHEAR FORCE (KN)				
OUTER GIRDER				
Combinations 18m Span 21m Span 24m Span				
Comb1	1078.14	1318.34	2949.63	
Comb2	865.69	1408.09	2693.46	



Chart-3. Comparison of combination and Shear force for different spans

From the graph it is observed that, when the span is more the Shear force will be more. Because when we increase length of the span changes, length of the span effects on this Shear force. Combination -1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Shear force value decreases for the live load Combination-2, As per IRC-6, it includes Class-A loading. The class-A loading is less compared to the 70R loading. When the vehicle load increases SF also increases.

. Table-3: Comparison of Shear force for Different Spans

SHEAR FORCE(kN)				
INNER GIRDER				
Combinations 18m Span 21m Span 24m Span				
Comb1	800.27	950.71	2179.30	
Comb2	725.57	1160.97	2085.03	



Chart-4: Comparison of combination and Shear force for different spans

From the graph it is observed that, when the span is more the Shear force will be more. Because when we increase length of the span changes, length of the span effects on this Shear force. Combination -1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Shear force value decreases for the live load Combination-2, As per IRC-6, it includes Class- A loading. The class-A loading is less compared to the 70R loading. When the vehicle load increases SF also increases.

c) Joint reaction force

Table-5: Comparison of Joint reaction force for DifferentSpans

JOINT FORCE REACTION(kN)			
Combinations	18m Span	21m Span	24m Span
Comb1	3209.72	2018.20	4802.10
Comb2	3013.61	2396.21	4671.88



Chart-5: Comparison of combination and joint reaction force for different spans

It is observed from the graph that, Joint reaction at a support increases when the span increases. Joint reaction at the support is more for live load combination-1 as compared to the live load combination-2.

For THREE Lane analysis

a) Bending moment

Table-6:Comparison of Bending moment for DifferentSpans

BENDING MOMENT(kN-M)				
OUTER GIRDER				
Combinations	18m span	21m span	24m span	
Comb1	3559.47	6930.32	9763.17	
Comb2	2932.24	6437.47	8793.89	
Comb3	4544.48	8461.51	11220.49	



Chart-6: Comparison of combination and Bending moment for different spans

From the graph it is observed that, when the span is more the Bending moment will be more. Because when we increase length of the span changes, length of the span effects on this Bending moment. Combination-1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Bending moment value decreases for the live load Combination-2, As per IRC-6, it includes Class- A loading. The class-A loading is less compared to the 70R loading. Combination-3 consisting both 70R and class-A loading. When the vehicle load increases BM also increases

Table-7:Comparison of Bending moment for Different Spans

BENDING MOMENT(kN-M)				
INNER GIRDER				
Combinations	18m span	21m span	24m span	
Comb1	2154.30	5043.76	6709.89	
Comb2	2158.22	5366.04	6904.03	
Comb3	3761.69	7215.84	9069.60	



Chart-7: Comparison of combination and Bending moment for different spans

It is seen from the above graph that, when the span is more the Bending moment will be more. Because when we increase length of the span changes, length of the span effects on this Bending moment. Combination-1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Bending moment value decreases for the live load Combination-2, As per IRC-6, it includes Class- A loading. The class-A loading is less compared to the 70R loading. Combination-3 consisting both 70R and class-A loading when the vehicle load increases BM also increases.

b) Shear force

Table-8: Comparison of Shear force for Different Spans

SHEAR FORCE(kN)				
OUTER GIRDER				
Combinations	18m Span	21m Span	24m Span	
Comb1	865.52	1357.93	1652.78	
Comb2	626.14	1173.77	1401.26	
Comb3	998.82	1563.03	1800.49	



Chart-8: Comparison of combination and Shear force for different spans

It is seen from the above graph that, when the span is more the Shear force will be more. Because when we increase length of the span changes, length of the span effects on this Shear force. Combination-1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Shear force value decreases for the live load Combination-2, As per IRC-6, it includes Class- A loading. The class-A loading is less compared to the 70R loading. Combination-3 consisting both 70R and class-A loading. When the vehicle load increases SF also increases. Table-9: Comparison of Shear force for Different Spans

SHEAR FORCE(kN)				
INNER GIRDER				
Combinations	18m Span	21m Span	24m Span	
Comb1	461.963	948.947	1124.523	
Comb2	462.482	975.957	1114.196	
Comb3	805.125	1350.402	1527.765	

Chart-9: Comparison of combination and Shear force for different spans

It is seen from the above graph that, when the span is more the Shear force will be more. Because when we increase length of the span changes, length of the span effects on this Shear force. Combination-1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Shear force value decreases for the live load Combination-2, As per IRC-6, it includes Class- A loading. The class-A loading is less compared to the 70R loading. Combination-3 consisting both 70R and class-A loading. When the vehicle load increases SF also increases.

c) Joint reaction force

 Table-10 :Comparison of Joint reaction force for Different

 Spans

JOINT REACTION FORCE(kN)			
Combinations	18m Span	21m Span	24m Span
Comb1	957.26	1977.98	2368.90
Comb2	948.29	2044.28	2380.69
Comb3	1378.22	2480.99	2821.89



Chart-10. Comparison of combination and Joint reaction force for different spans



It is observed from the graph that, Joint reaction at a support increases when the span increases. Joint reaction at the support is more for live load combination-3 as compared to the live load combination-1 and combination-2. Because live load combination includes IRC 70R with Class-A loading.

Tabulations of Results for Substructure

For Two Lane analysis

a) Base reaction

Table.11 Comparison of Base reaction for Different Spans

BASE REACTION(kN)			
Combinations	18m span	21m span	24m span
Comb1	3756.83	4578.12	10257.87
Comb2	3182.54	5138.14	9567.60



Chart-11: Comparison of combination and Base reaction for different spans

From the graph, it is observed that, when the span increases the Base reaction increases. Because when we increase length of the span changes, length of the span effects on this Base reaction. Combination -1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Base reaction value decreases for the live load Combination-2, As per IRC-6, it includes Class-A loading. The class-A loading is less compared to the 70R loading. When the vehicle load increases Base reaction also increases.

b) Bending moment

Table-12: Comparison of Bending moment for DifferentSpans

BENDING MOMENT(kN-M)					
PIER CAP					
Combinations 18m span 21m span 24m span					
Comb1	4320.00	5218.83	11796.54		
Comb2	3659.91	5908.85	10990.55		



Chart-12: Comparison of combination and Bending moment for different spans

From the graph, when the span is more the Bending moment will be more. Because when we increase length of the span changes, length of the span effects on this Bending moment. Combination -1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Bending moment value decreases for the live load Combination-2, As per IRC-6, it includes Class- A loading. The class-A loading is less compared to the 70R loading. When the vehicle load increases BM also increases.

Table-13:Comparison of Bending moment for Different Spans

BENDING MOMENT (kN-M)				
PIER				
Combinations	18m span	21m span	24m span	
Comb1	0000000367	00000002320	00000007611	
Comb2	00000001843	0000000002622	00000006769	



Chart-13:Comparison of combinations and Bending moment for different spans

From the graph, when the span is more the Bending moment will be more. Because when we increase length of the span changes, length of the span effects on this Bending moment. Combination -1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Bending moment value decreases for the live load Combination-2, As per IRC-6, it includes Class- A loading. The class-A loading is less compared to the 70R loading. When the vehicle load increases BM also increases.

c) Shear force

Table-14: Comparison of Shear force for DifferentSpans

SHEAR FORCE(KN)				
PEIR CAP				
Combinations	18m span	21m span	24m span	
Comb1	1878.42	2269.05	5128.93	
Comb2	1591.269	2569.06	4778.50	



Chart-14:Comparison of combination and Shear force for different spans

From the graph it is observed that, when the span is more the Shear force will be more. Because when we

increase length of the span changes, length of the span effects on this Shear force. Combination -1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Shear force value decreases for the live load Combination-2, As per IRC-6, it includes Class-A loading. The class-A loading is less compared to the 70R loading. When the vehicle load increases SF also increases.

Table-15 : Comparison of Shear force for Different Spans

SHEAR FORCE(kN)				
PIER				
Combinations	18m span	21m span	24m span	
Comb1	3756.82	4578.12	10252.87	
Comb2	3182.54	5138.14	9567.60	



Chart-15: Comparison of combination and Shear force for different spans

From the graph it is observed that, when the span is more the Shear force will be more. Because when we increase length of the span changes, length of the span effects on this Shear force. Combination -1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Shear force value decreases for the live load Combination-2, As per IRC-6, it includes Class- A loading. The class-A loading is less compared to the 70R loading. When the vehicle load increases SF also increases. International Research Journal of Engineering and Technology (IRJET)e-ISSN: 2395-0056Volume: 05 Issue: 08 | Aug 2018www.irjet.netp-ISSN: 2395-0072

For THREE Lane analysis

a) Base reaction

Table-16: Comparison of Base reaction for Different Spans

BASE REACTION (kN)			
Combinations	18m span	21m span	24 m span
Comb1	2654.96	4613.76	5554.62
Comb2	2177.26	4299.44	5030.92
Comb3	3607.88	5826.84	6656.51



Chart-16:Comparison of Base reaction for different spans

From the graph it is observed that, when the span is more the Base reaction will be more. Because when we increase length of the span changes, length of the span effects on this Base reaction. Combination-1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Bending moment value decreases for the live load Combination-2, As per IRC-6, it includes Class- A loading. The class-A loading is less compared to the 70R loading. Combination-3 consisting both 70R and class-A loading. When the vehicle load increases Base reaction also increases.

b) Bending moment

 Table-17 :Comparison of Bending moment for Different

 Spans

BENDING MOMENT (kN-M)			
PIER CAP			
Combinations	18m span	21m span	24m span
Comb1	3053.20	5305.82	6387.81
Comb2	2503.24	4944.35	5785.55
Comb3	4149.06	6700.86	7654.93



Impact Factor value: 7.211 |



Chart-17: Comparison of combination and Bending moment for different spans

From the graph it is observed that, when the span is more the Bending moment will be more. Because when we increase length of the span changes, length of the span effects on this Bending moment. Combination-1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Bending moment value decreases for the live load Combination-2, As per IRC-6, it includes Class A loading. The class-A loading is less compared to the 70R loading. Combination-3 consisting both 70R and class-A loading. When the vehicle load increases BM also increases.

Table-18: Comparison of Bending moment for DifferentSpans

BENDING MOMENT (kN-M)				
PIER				
Combinations	18m span	21m span	24m span	
Comb1	000000000909	00000003935	00000005022	
Comb2	00000001364	00000003571	00000004587	
Comb3	00000001819	00000004682	000000006103	



Chart-18:Comparison of combination and Bending moment for different spans

From the graph it is observed that, when the span is more the Bending moment will be more. Because when we increase length of the span changes, length of the span effects on this Bending moment. Combination-1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Bending moment value decreases for the live load Combination-2, As per IRC-6, it includes Class- A loading. The class-A loading is less compared to the 70R loading. Combination-3 consisting both 70R and class-A loading. When the vehicle load increases BM also increases.

c) Shear force

Table-19: Comparison of Shear force for Different Spans

SHEAR FORCE (kN)			
PEIR CAP			
Combinations	18m span	21m span	24m span
Comb1	1327.48	2306.88	2775.31
Comb2	1088.62	2149.72	2515.46
Comb3	1803.94	2913.42	3328.25



Chart-19.:Comparison of combination and Shear force for different spans

It is seen from the above graph that, when the span is more the Shear force will be more. Because when we increase length of the span changes, length of the span effects on this Shear force. Combination-1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Shear force value decreases for the live load Combination-2, As per IRC-6, it includes Class- A loading. The class-A loading is less compared to the 70R loading. Combination-3 consisting both 70R and class-A loading. When the vehicle load increases SF also increases. Table-20: Comparison of Shear force for Different Spans

SHEAR FORCE (kN)			
PIER			
Combinations	18m span	21m span	24m span
Comb1	2654.96	4613.76	5554.62
Comb2	2177.76	4299.44	5030.92
Comb3	3607.88	5826.84	6656.51



Chart-20: Comparison of combination and Shear force for different spans

It is seen from the above graph that, when the span is more the Shear force will be more. Because when we increase length of the span changes, length of the span effects on this Shear force. Combination-1 as per IRC-6. The combination of live load for this condition involves 70R loading. According to IRC-6, 70R loading is more compared to other loading. When the Shear force value decreases for the live load Combination-2, As per IRC-6, it includes Class- A loading. The class-A loading is less compared to the 70R loading. Combination-3 consisting both 70R and class-A loading. When the vehicle load increases SF also increases.

5. CONCLUSIONS

An attempt has been made to grillage analysis for 18m,span. Totally eight models have done in super structure and substructure. Grillage analysis are considered for IRC 70R and class-A loading.

- When the span increases, Bending moment and Shear force also increases.
- In two lane analysis, Bending moment and Shear force of 31.59%,29.34%,28.49% and 25.77%, 27.12%,26.12% is more in outer girder compared to inner girder.
- In three lane analysis, Bending moment and Shear force of 39.48% ,27.22% 31.27% and 46.63%, 30.12%, 31.96% is more in outer girder compared to inner girder.



Combination-3 consisting IRC 70R loading with class-A loading. When the vehicle load increases, Shear force and bending moment also increases.

- \geq In both two lane and three lane analysis, 17.22%, 63.38% and 42.46%, 52.20% of Bending moment is more in pier cap than pier.
- In both two lane and three lane analysis, \geq 17.22%,63.38% and 42.46%,52.17% of shear force is more in pier cap than pier.

ACKNOWLEDGEMENT

The authors wish to thank the authorities of Visveswaraya Technological University, Belgaum for giving us an opportunity to conduct the analytical work in the CAD laboratory of University B.D.T College of Engineering. Davangere 577004.

REFERENCES

[1] Anushia K Ajay, Asha U Rao, N.A. PremanandShenoy" Parametric study on T-beam Bridge" - International Journal of Civil Engineering and Technology (IJCIET) ISSN: 0976-6308, *Volume-08, Issue-06, [June 2017]*

[2] Sudarshanprabhakarpatil, KameshwarRaoTallapragada "Analysis and Design if R.C.C T-beam girder Bridge using IRC Class AA and Class A Loading" -International Journal of Engineering Research in Mechanical and Civil Engineering (IJERMCE) ISSN: 2546-1290, Volume-02, Issue-03, [March 2017]

[3] OmkarVelhal J.P Patankar "Study of R.C.C T-beam Bridge with Skew Angle " -International Journal of Innovative Research in Science, Engineering and Technology (IJIRSET) ISSN: 2347-6710, Volume-05, Issue-06, [June 2016]

[4] Sandeshupadhyaya K, F. Sathaya Sachin "A Comparative Study of T- Beam Bridges for varying span lengths" -International Journal of Research in Engineering and Technology (IJRET) ISSN: 2321-7308, Volume-05, Issue-06, [June 2016]

[5] Mahantesh.S. Kamatagi, Prof. M. Manjunath "Comparative Study of design of longitudinal girder of T- beam Bridge Using IRC 21-2000 & IRC 112- 2011" -International Research Journal of Engineering and Technology (IRJET) ISSN: 2395-0072, Volume-02, Issue-06, [Sept 2015]

[6] R.Shareedhar, ShivanandTenagi "Comparative study of Tbeam bridge longitudinal girder design using IRC 112:2011 and IRC 21:2000" -International Journal of Scientific and Engineering Research (IJSER) ISSN: 2229-5518 Volume-06, Issue-08, [Aug 2015]

[7] SupriyaMadda, Kalyanshetti M.G "Dynamic analysis of Tbeam Bridge Superstructure" - International Journal of Civil and Structural Engineering (IJCSE) ISSN: 0976-4399, Volume-03, Issue-03, [March 2013]

[8] AmitSavena, Dr.SavithaMaru "Comparative study of Analysis and Design of T-beam girder and Box girder superstructure" -International Journal of Research in Engineering & Advanced Technology (IJREAST) ISSN: 2320-8791, Volume-01, Issue-02, [May 2013]

[9] R. ShreedharSpurtiMamadapur "Analysis of T-beam Bridge using Finite element method" International Journal of Engineering and Innovative Technology (IJEIT) ISSN: 2277-3754, volume-02, Issue-03, [September 2012]

[10] IRC-6-2014- "Standard Specifications and code of practice for Road Bridges". Indian road congress, Published by New Delhi.

[11] IS: 456-2000 – Code of practice for plain and Reinforced concrete, Fourth Revision.

[12] N.KrishnaRaju, Design of Bridges, 4 Edition, 2013